

#### What is claimed is:

- 1. A precoder for generating a mapped constellation signal from an input signal,
- 2 comprising:
- a feedback filter that generates a feedback signal as a function of the mapped
- 4 constellation signal, and
- 5 a discrete modulo adder that generates the mapped constellation signal from the input
- 6 signal and the feedback signal, the discrete modulo adder utilizing an index to the constellation
- of levels chosen for the precoder, such that the amplitude of the mapped constellation signal is
- 8 limited.

1

4

5

1

- 2. The precoder according to claim 1, wherein the discrete modulo adder comprises:
- an adder that adds together the feedback signal and the input signal to generate a
- 3 partial result, and
  - a mapper that generates the mapped constellation signal by mapping a partial result
    - outside a basic constellation of levels onto the basic constellation of levels as a function of the
- 6 index to the constellation of levels for the precoder.
- 1 3. The precoder according to claim 1, wherein the feedback filter includes a delay
- 2 element and a weighting element such that the feedback filter multiplies a delayed version of
- 3 the mapped constellation signal by the weighting element to generate the feedback signal.
- 4. The precoder according to claim 1, wherein the feedback filter is based upon a
- 2 model of the impulse response of a communication channel.
  - 5. The precoder according to claim 2, wherein the mapper further comprises:

2	a table identifying a basic c	onstellation of levels and a mapping from levels outside the
3	basic constellation to levels inside	the basic constellation.

- 6. The precoder according to claim 5, wherein each of the levels outside the basic constellation in the table are mapped onto only one level inside the basic constellation in the table.
  - 7. The precoder according to claim 5, further comprising:
- a table having a constellation index basic\_const, where basic\_const goes from 1 to k, associated with each of a plurality of levels inside the basic constellation, and having a constellation index positive\_const, where positive\_const goes from k+1 to m, associated with a plurality of levels outside the basic constellation.
- 8. The precoder according to claim 7, wherein each of the plurality of levels outside the basic constellation index are mapped onto a level inside the basic constellation according to the equation:
  - index positive\_const  $\rightarrow$  positive\_const (2\*k); while positive\_const > m-k; and index positive\_const  $\rightarrow$  positive\_const (2\*k) -1; while positive\_const <= m-k; wherein  $\rightarrow$  identifies the mapping function.
  - 9. The precoder according to claim 5, further comprising:
- a table having a constellation index basic\_const, where basic\_const goes from -1 to -k, associated with each of a plurality of levels inside the basic constellation, and having a constellation index negative\_const, where negative\_const goes from -k-1 to -m, associated with a plurality of levels outside the basic constellation.



1	10. 'The precoder according to claim 9, wherein each of the plurality of levels outside
2	the basic constellation index are mapped onto a level inside the basic constellation according
3	to the equation:
4	index negative_const → negative_const + (2*k); while negative_const < -(m-k); and
5	index negative_const $\rightarrow$ negative_const + (2*k) +1; while negative_const >= -(m-k);
6	wherein → identifies the mapping function.
1	11. The precoder according to claim 7, wherein the mapper further comprises a

- 11. The precoder according to claim 7, wherein the mapper further comprises a comparator for comparing the partial result with the levels in the table.
  - 12. The precoder according to claim 11, wherein the comparator identifies the level closest to the partial result.
  - 13. The precoder according to claim 12, wherein the mapper further includes an output block that generates a mapped constellation signal equal to a level inside the basic constellation, if the identified level in the table closest to the partial result is inside the basic constellation.
  - 14. The precoder according to claim 12, wherein the output block includes a summer for adding the partial result and a mapping distance signal, wherein the mapping distance signal equals the distance between the index basic\_const, associated with the basic constellation level of the input signal, and the index positive\_const, associated with a level outside the basic constellation.
- 1 15. The precoder according to claim 1, further comprising a digital to analog converter 2 that generates an analog output signal based upon the mapped constellation signal.

1	16. The precoder according to claim 15, further comprising a transformer for operably
2	coupling the digital to analog converter to an analog subscriber loop.
1	17. The precoder according to claim 15, wherein successive levels in the basic
2	constellation are separated by a distance D1, and wherein a plurality of successive levels
3	outside the basic constellation are separated by a distance D2 such that D1 differs from D2.
1	18. A precoder for an analog modem, the precoder comprising:
2	a discrete modulo adder that generates a mapped constellation signal as a function of a
3	feedback signal and an input signal to the precoder, the discrete modulo adder including:
4	an adder that adds together the feedback signal and the input signal to generate
5	a partial result,
6	a table identifying a basic constellation of levels and levels outside the basic
7	constellation, wherein the levels outside the basic constellation are mapped onto levels inside
8	the basic constellation as a function of an index associated with each level in the table,
9	a comparator for comparing the partial result with the levels in the table,
10	an output block that generates a mapped constellation signal equal to a level
11	inside the basic constellation by mapping a partial result outside the basic constellation of
12	levels onto a level inside the basic constellation of levels, and
13	a feedback filter that generates the feedback signal as a function of the mapped
14	constellation signal output by the discrete modulo adder.
1	19. The precoder according to claim 18, wherein each of the levels outside the basic
2	constellation in the table are mapped onto only one level inside the basic constellation in the
3	table.

1	20. The precoder according to claim 16, further comprising
2	a table having a constellation index basic_const, where basic_const goes from 1 to k,
3	associated with each of a plurality of levels inside the basic constellation, and having a
4	constellation index positive_const, where positive_const goes from k+1 to m, associated with
5	a plurality of levels outside the basic constellation.
1	21. The precoder according to claim 20, wherein each of the plurality of levels outside
2	the basic constellation index are mapped onto a level inside the basic constellation according
3	to the equation:
4	index positive_const → positive_const - (2*k); while positive_const > m-k; and
5	index positive_const $\rightarrow$ positive_const $-(2*k) -1$ ; while positive_const $\leq$ m-k;
6	wherein → identifies the mapping function.
1	22. The precoder according to claim 18, further comprising:
2	a table having a constellation index basic_const, where basic_const goes from -1 to -k
.3	associated with each of a plurality of levels inside the basic constellation, and having a
4	constellation index negative_const, where negative_const goes from -k-1 to -m, associated
5	with a plurality of levels outside the basic constellation.
1	23. The precoder according to claim 22, wherein each of the plurality of levels outside
2	the basic constellation index are mapped onto a level inside the basic constellation according
3	to the equation:
4	index negative_const → negative_const + (2*k); while negative_const < -(m-k); and
5	index negative_const → negative_const + (2*k) +1; while negative_const >= -(m-k);
6	wherein → identifies the mapping function.
	3 4 5 1 2 3 4 5 6 1 2 3 4 5 1 2 3 4 5 5 1 2

1	24. The precoder according to claim 20, wherein the output block includes a summer
2	for adding the partial result and a mapping distance signal, wherein the mapping distance
3	signal equals the distance between the index basic_const, associated with the basic
4	constellation level of the input signal, and the index positive_const, associated with a level
5	outside the basic constellation.
1	25. A method of precoding an input signal to generate a mapped constellation signal,
2	comprising:
3	generating a feedback signal from the mapped constellation signal, and
4	performing a discrete modulo operation on the feedback signal and the input signal
5	based upon an index to the constellation of levels chosen for the precoder, such that the
6	amplitude of the mapped constellation signal is limited.
1	26. The method of precoding according to claim 25, wherein the step of performing a
2	discrete modulo operation includes:
3	adding together the input signal and the feedback signal to generate a partial
4	result,
5	determining whether the generated partial result is contained within a basic
6	constellation of levels, and
7	generating the mapped constellation signal by mapping a partial result outside the basic
8	constellation of levels onto a level inside the basic constellation of levels as a function of the
9	index to the constellation of levels for the precoder.
	· ·

	4
1	27. The method according to claim 25, wherein the step of generating the feedback
2	signal further includes multiplying a delayed version of the mapped constellation signal by a
3	weighting element to generate the feedback signal.
1	28. The method according to claim 26, wherein the determining step further includes
2	comparing the generated partial result with a table identifying a basic constellation of levels
3	and a plurality of levels outside the basic.
1	29. The method according to claim 28, further including generating a mapped
2	constellation signal equal to the partial result if the partial result is inside the basic
3	constellation of levels.
1	30. The method according to claim 28, further including the step of determining
2	whether the partial result is less than the minimum level of the basic constellation or whether
3	the partial result is greater than the maximum level of the basic constellation.
1	31. The method according to claim 30, further including the step of determining a
2	mapping distance p <sub>j</sub> when the partial result is less than the minimum level of the basic
3	constellation, the mapping distance $p_j$ being equal to a distance between an index basic_const,
4	associated with the basic constellation level of the input signal, and an index positive_const,
5	associated with a level outside the basic constellation.
1	32. The method according to claim 31, wherein the index positive_const is an index to
2	a level that maps onto the basic constellation level of the input signal, and wherein index
3	positive_const is an index to a level in a positive constellation of levels that includes those
4	levels greater than the maximum level in the basic constellation.

1	33. The method according to claim 32, further including the step of obtaining the index
2	positive_const from a table.
1	34. The method according to claim 31, further including the step of generating a
2	mapped constellation signal by adding together the partial result and the mapping distance $p_j$ .
1	35. The method according to claim 30, further including the step of determining a
2	mapping distance n <sub>j</sub> when the partial result is greater than the maximum level of the basic
3	constellation, the mapping distance n <sub>j</sub> being equal to a distance between an index basic_const,
4	associated with the basic constellation level of the input signal, and an index negative_const,
5	associated with a level outside the basic constellation.
1	36. The method according to claim 35, wherein the index negative_const is an index to
2	a level that maps onto the basic constellation level of the input signal, and wherein index
3	negative_const is an index to a level in a negative constellation of levels that includes those
4	levels less than the minimum level in the basic constellation.
1	37. The method according to claim 36, further including the step of obtaining the index
2	negative_const from a table.
1	38. The method according to claim 35, further including the step of generating a
2	mapped constellation signal by adding together the partial result and the mapping distance $n_{j}$ .
1	39. A computer-readable medium having stored thereon a plurality of instructions, the
2	plurality of instructions including instructions that when executed by a processor cause the
3	processor to implement a method of precoding an input signal to generate a mapped
4	constellation signal, the method comprising:
5	generating a feedback signal from the mapped constellation signal, and
	· ·

	1
6	performing a discrete modulo operation on the feedback signal and the input
7	signal based upon an index to the constellation of levels chosen for the precoder, such that the
8	amplitude of the mapped constellation signal is limited.
1	40. The computer-readable medium of claim 39, wherein the step of performing a
2	discrete modulo operation further includes:
3	adding together the input signal and the feedback signal to generate a partial result,
4	determining whether the generated partial result is contained within a basic
5	constellation of levels, and
5	generating the mapped constellation signal by mapping a partial result outside the basic
7	constellation of levels onto a level inside the basic constellation of levels.
	Ada A